Sharpening the empirical claims of generative syntax through formalization

Tim Hunter

University of Minnesota, Twin Cities

NASSLLI, June 2014

Part 1: Grammars and cognitive hypotheses

- What is a grammar?
- What can grammars do?
- Concrete illustration of a target: Surprisal

Parts 2–4: Assembling the pieces

- Minimalist Grammars (MGs)
- MGs and MCFGs
- Probabilities on MGs

Part 5: Learning and wrap-up

- Something slightly different: Learning model
- Recap and open questions

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Part 1

Grammars and Cognitive Hypotheses

Outline

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Claims made by grammars

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Often tempting to draw a distinction between "linguistic evidence" (where grammar lives) and "experimental evidence" (where cognition lives)

- One need not make this distinction
- We will proceed without it, i.e. it's all linguistic (and/or all experimental)

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  - Why does it seem like a cop-out?
  - Lingering externalism/Platonism?
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  - Why does it seem like a cop-out?
  - Lingering externalism/Platonism?
  - Perhaps partly because it's just relatively rare to see anything being tested by other measures
- For another, we can incorporate grammars into claims that are testable by other measures.
  - This is the main point of the course!
  - The claims/predictions will depend on internal properties of grammars, not just what they say is good and what they say is bad
  - And we'll do it without seeing grammatical derivations as real-time operations

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[S]ince a competence theory must be incorporated in a performance model, evidence about the actual organization of behavior may prove crucial to advancing the theory of underlying competence.

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Evidence about X can only advance Y if Y makes claims about X!

Preview

What we will do:

- Put together a chain of linking hypotheses that bring "experimental evidence" to bear on "grammar questions"
  - e.g. reading times, acquisition patterns
  - e.g. move as distinct operation from merge vs. unified with merge
- Illustrate with some toy examples

What we will not do:

- Engage with state-of-the-art findings in the sentence processing literature
- End up with claims that one particular set of derivational operations is empirically better than another

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We'll take pairs of equivalent grammars that differ only in the move/re-merge dimension.

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The issues become "distant but empirical questions". That's all we're aiming for, for now.

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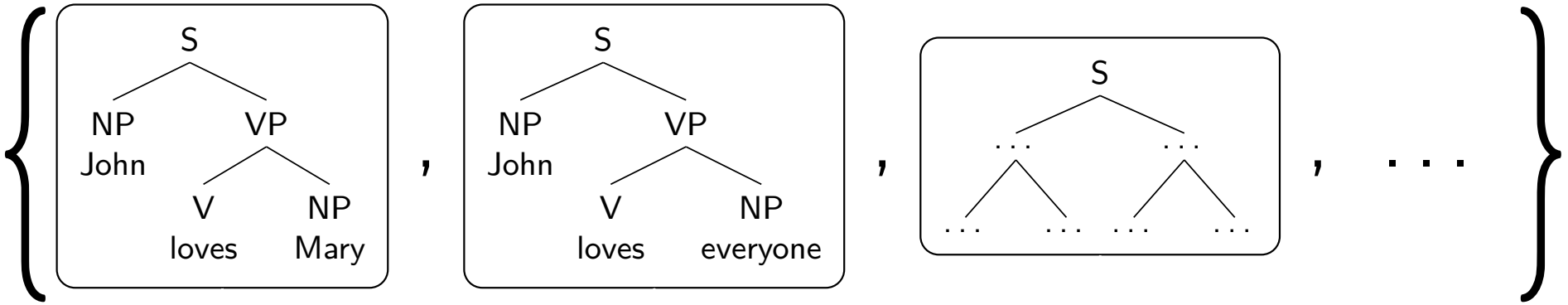
Interpretation functions



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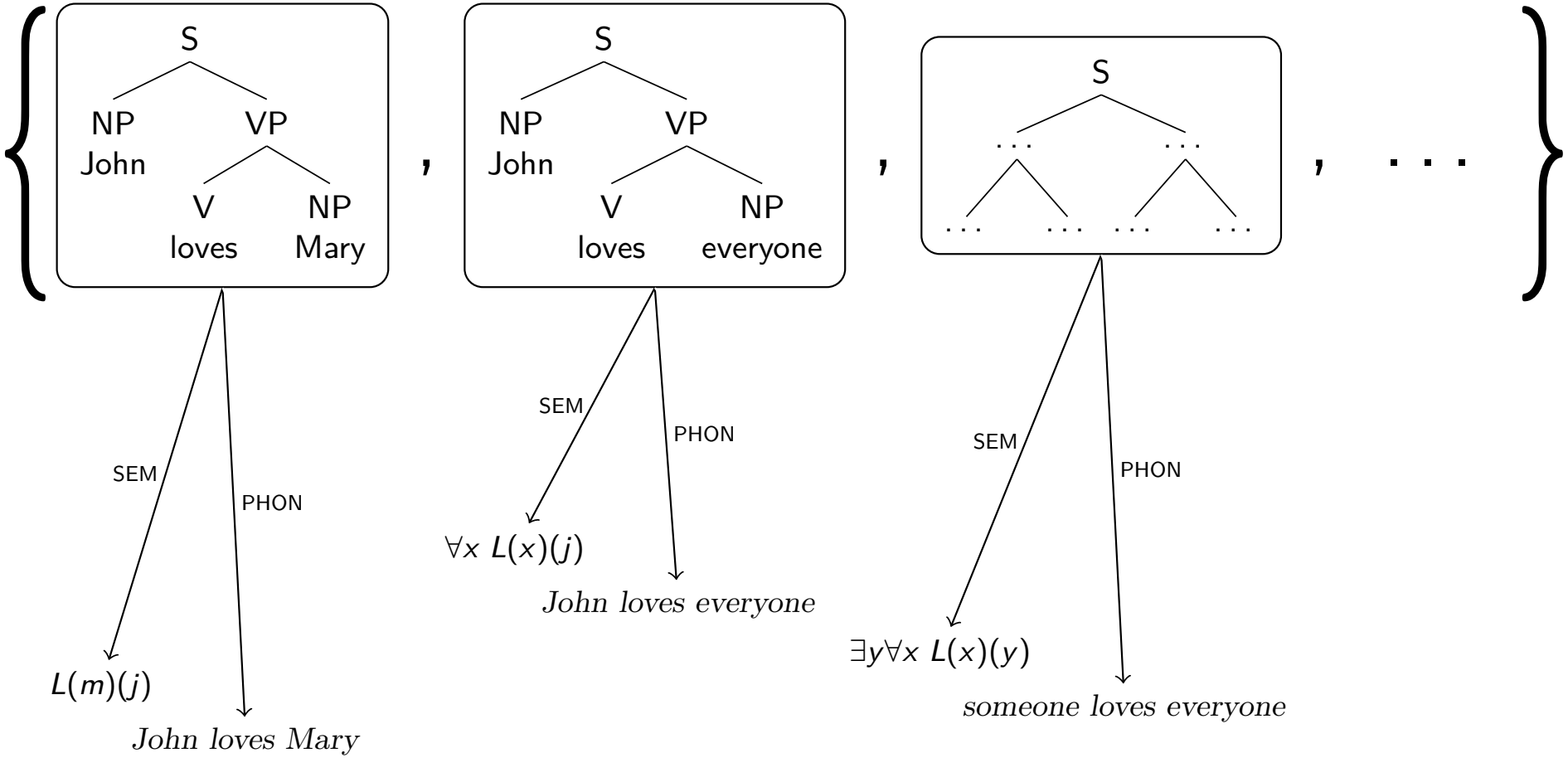

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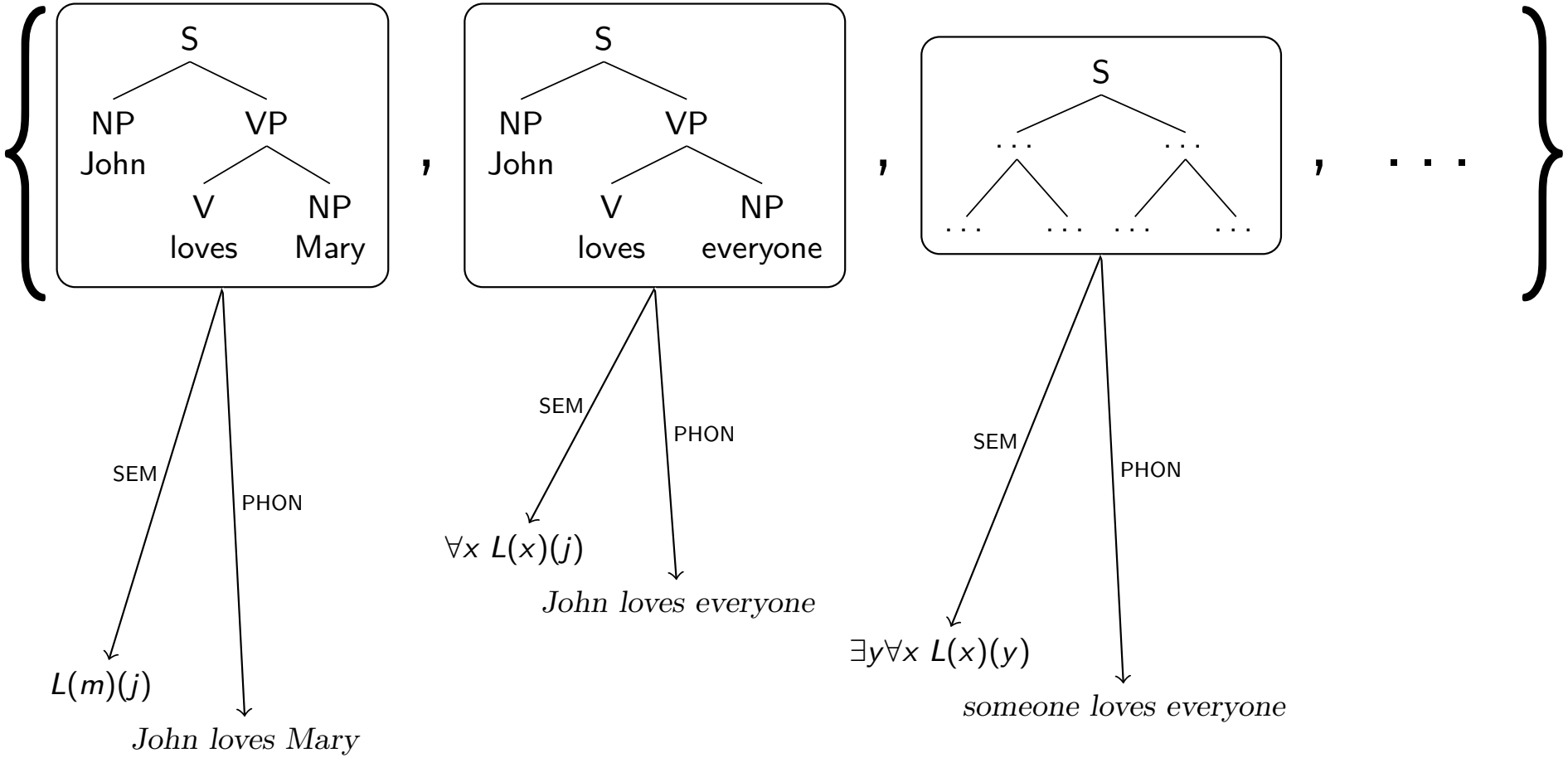

Caveats:

- Maybe we're interested in the finite specification of the set
- Maybe there's no clear line between observable and not
- Maybe some evidence is based on relativities among interpretations

Telling grammars apart

So, what if we have two different grammars — systems that define different sets of objects — that we can't tell apart via the sound and meaning interpretations?

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- Option 1: Conclude that the differences are irrelevant to us (or "they're not actually different").
- Option 2: Make the differences matter . . . somehow . . .

What are syntactic representations for?

Morrill (1994) in favour of Option 1:

> *The construal of a language as a collection of signs [sound-meaning pairs] presents as an investigative task the characterisation of this collection. This is usually taken to mean the specification of a set of "structural descriptions" (or: "syntactic structures"). Observe however that on our understanding a sign is an association of prosodic [phonological] and semantic properties. It is these properties that can be observed and that are to be modelled. There appears to be no observation which bears directly on syntactic as opposed to prosodic and/or semantic properties, and this implies an asymmetry in the status of these levels.* ***A structural description is only significant insofar as it is understood as predicting prosodic and semantic properties (e.g. in interpreting the yield of a tree as word order). Attribution of syntactic (or prosodic or semantic) structure does not of itself predict anything.***

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Where might we depart from this (to pursue Option 2)?

- Object that syntactic structure **does** matter "of itself"
- Object that prosodic and semantic properties are **not** the only ones we can observe

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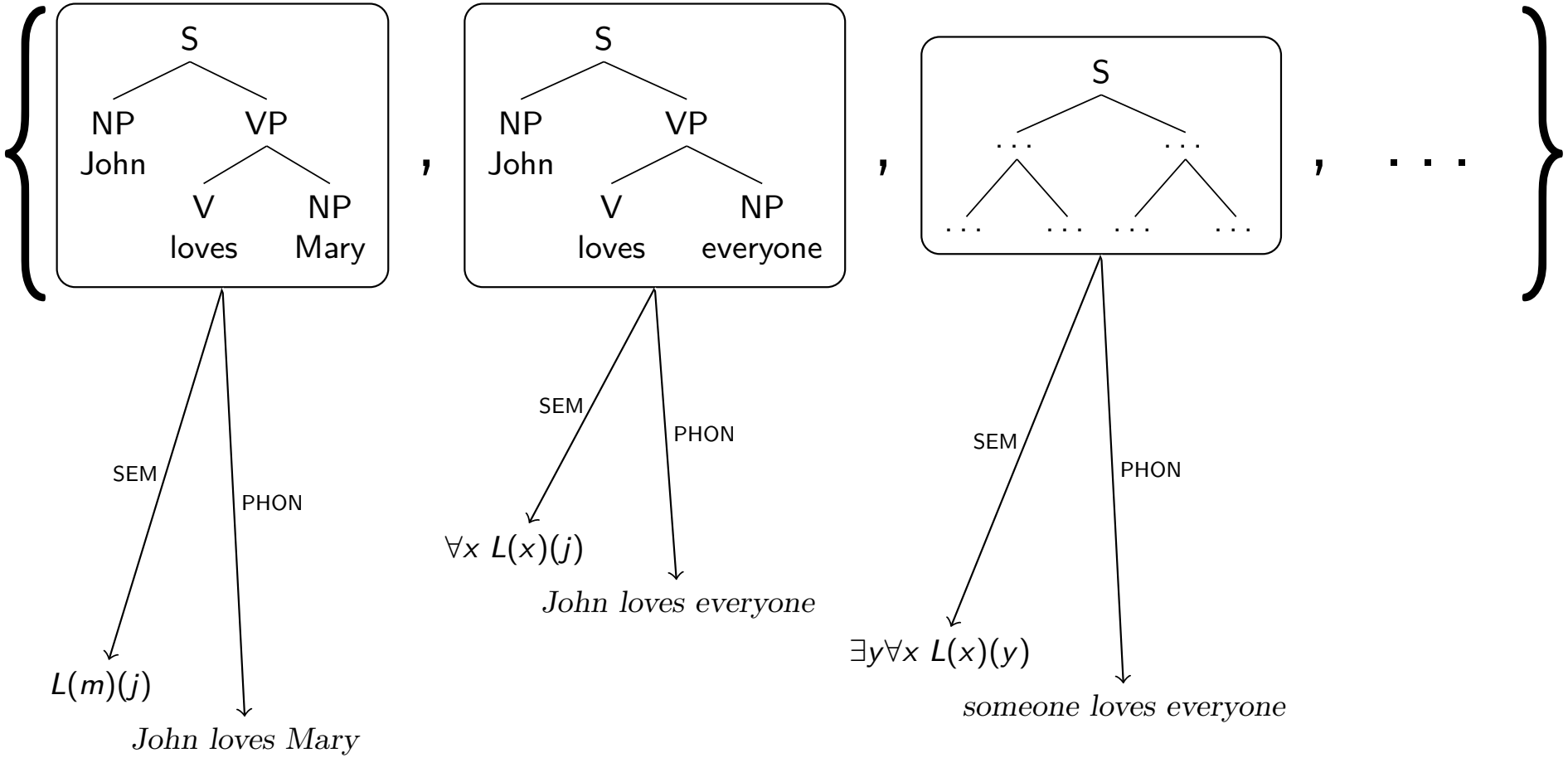

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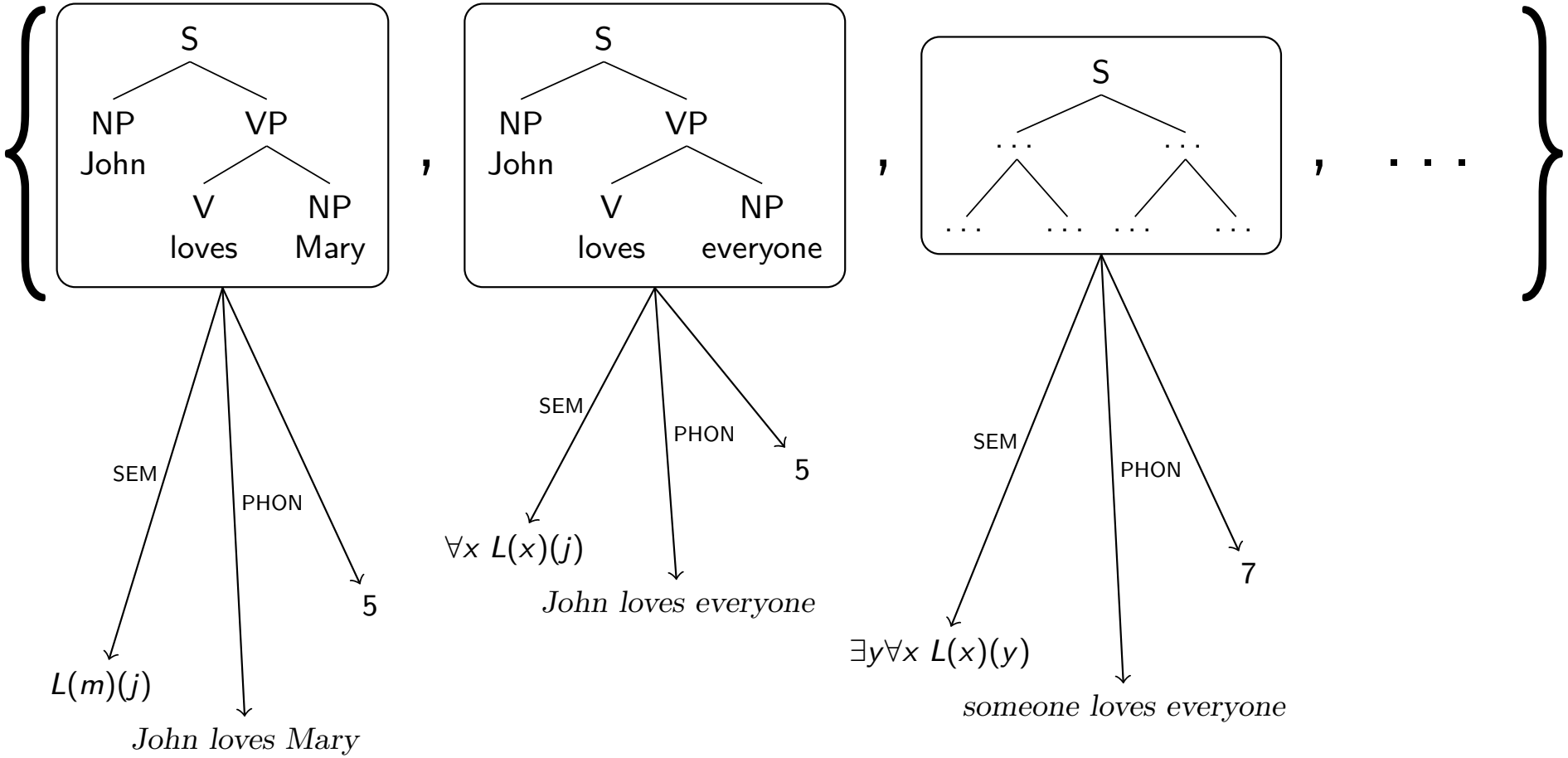

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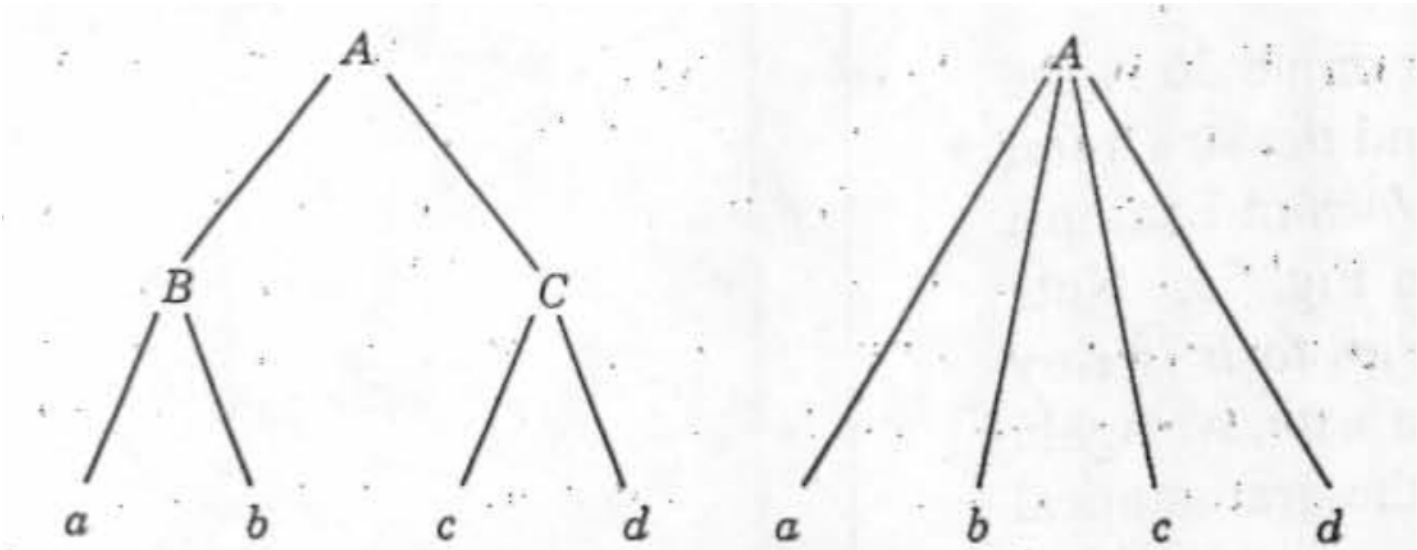
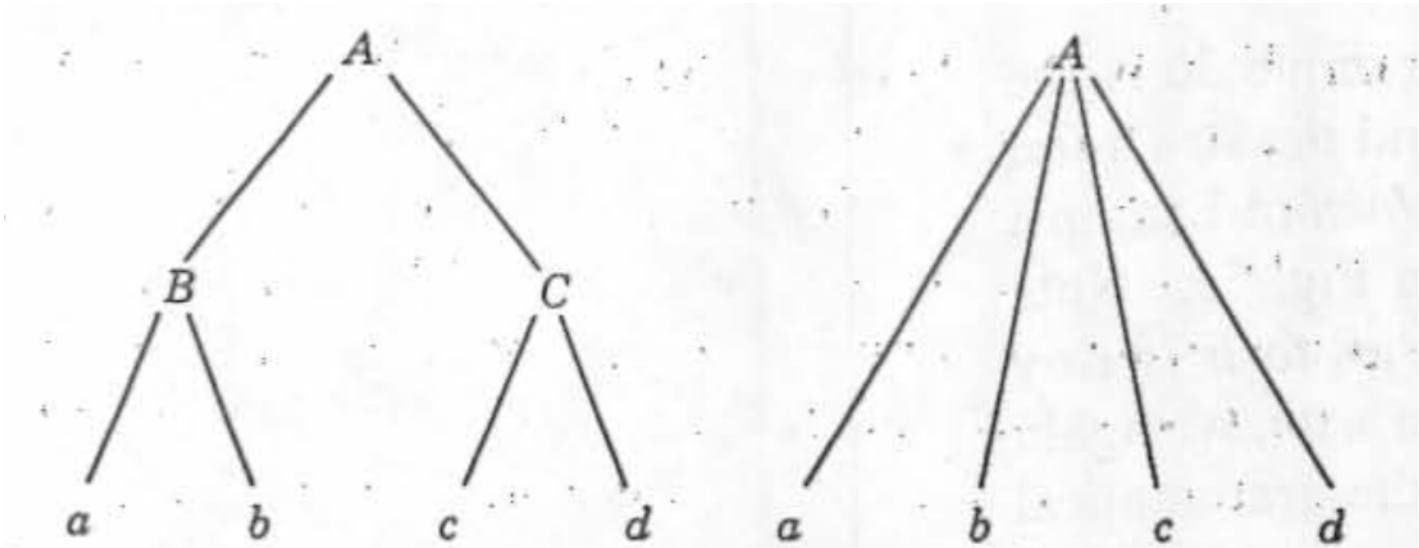


Fig. 8. Illustrating a measure of structural complexity. $N(Q)$ for the P-marker (a) is 7/4; for (b), $N(Q) = 5/4$.

(Miller and Chomsky 1963)

Ratio of total nodes to terminal nodes



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Won't distinguish center-embedding from left- and right-embedding

(1) The mouse [the cat [the dog bit] chased] died. (center)

(2) The dog bit the cat [which chased the mouse [which died]]. (right)

(3) [[the dog] 's owner] 's friend (left)

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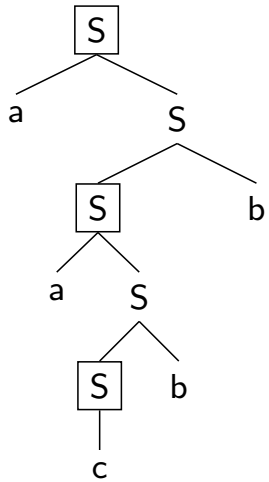
Degree of (centre-)self-embedding

A tree's degree of self-embedding is m iff:
"there is . . . a continuous path passing through $m + 1$ nodes $N_0, \ldots, N_m$, each with the same label, where each N_i $(i \geq 1)$ is fully self-embedded (with something to the left and something to the right) in the subtree dominated by N_{i-1}"



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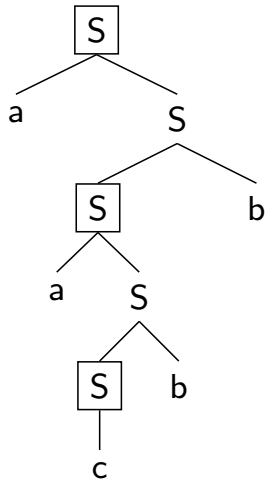

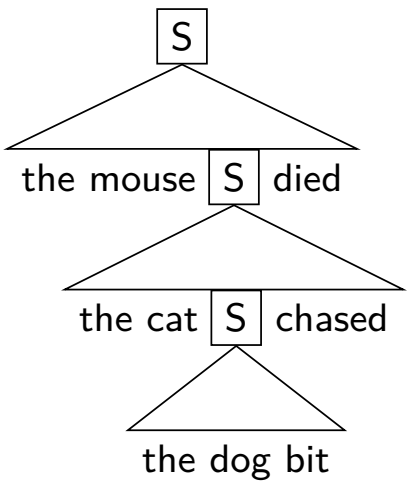

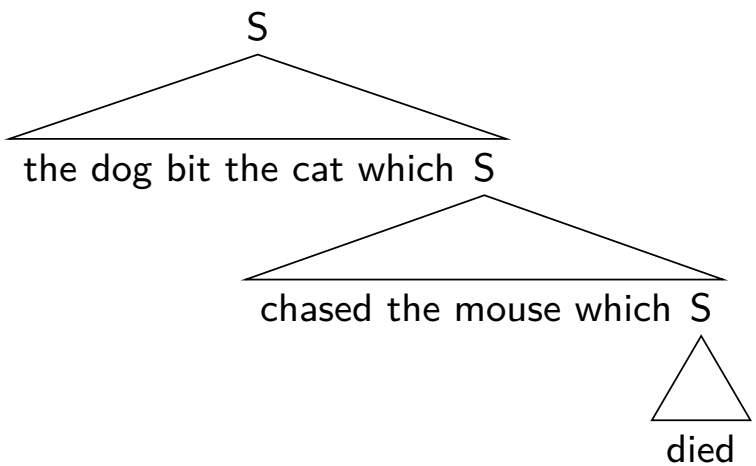

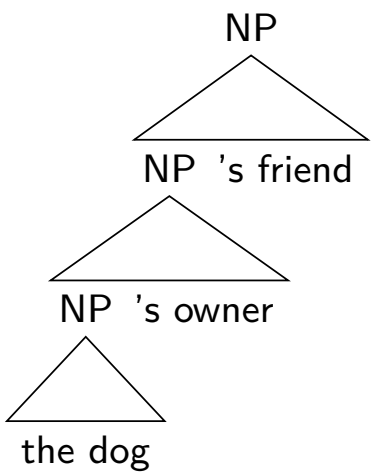

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Yngve's depth

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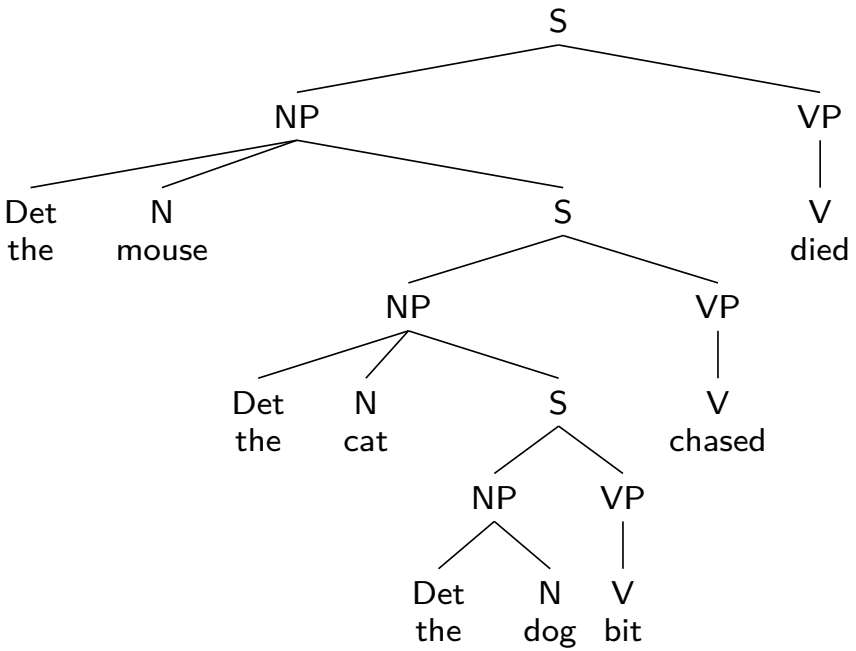

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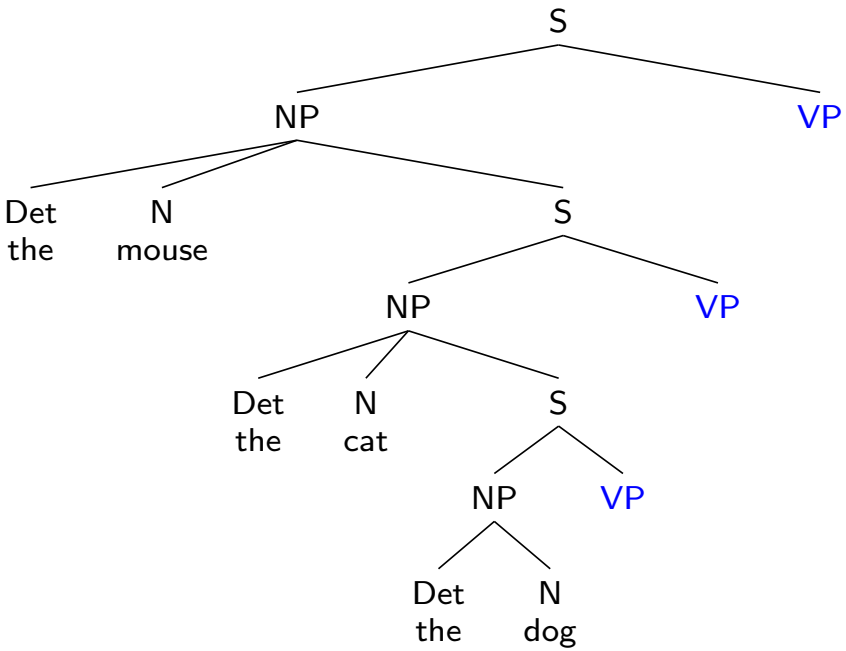

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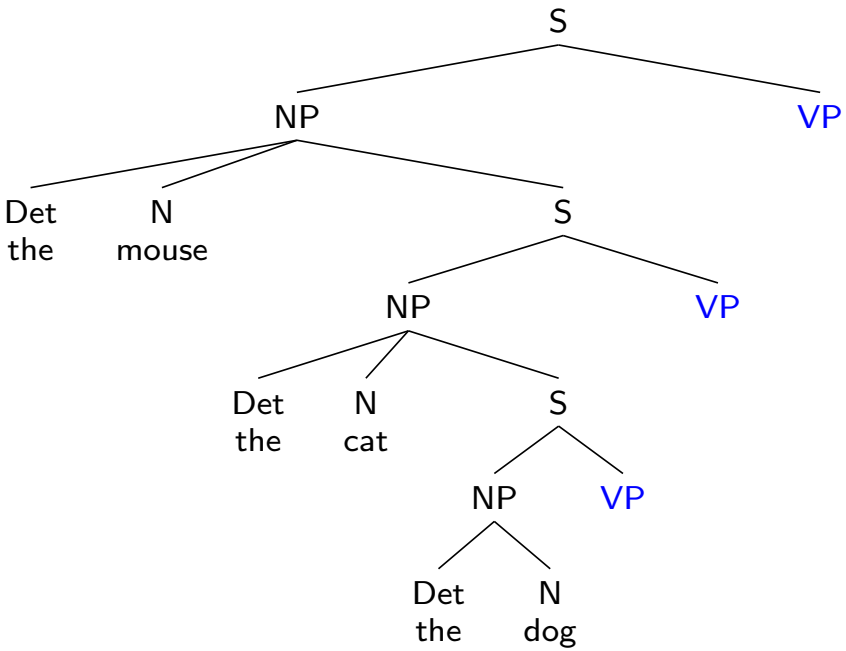

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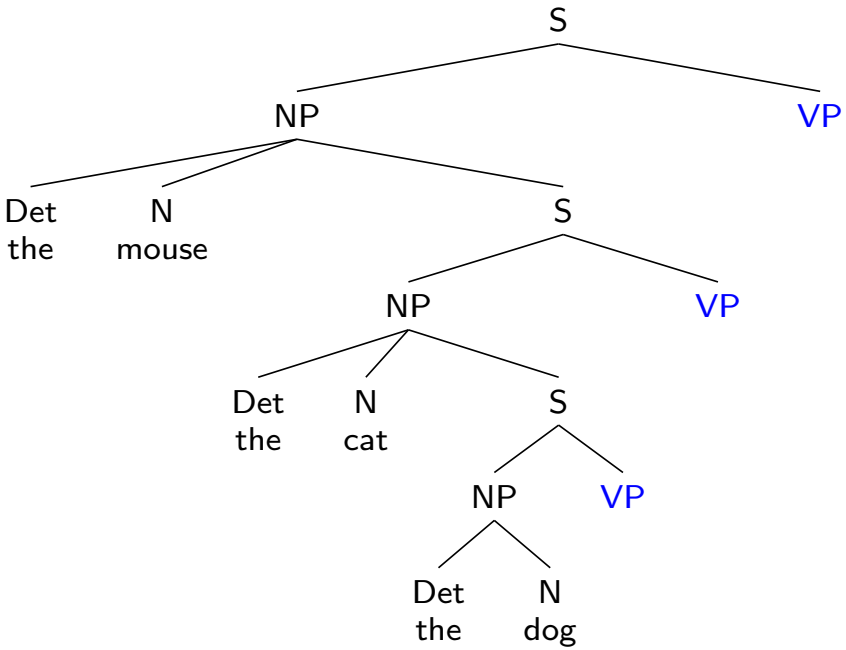

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- Yngve's theory was set within — perhaps justified by — a procedural story, but we can arguably detach it from that and treat depth as just another property of trees.

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$$\text{complexity metric} \quad + \quad \text{grammar} \quad \longrightarrow \quad \text{prediction}$$

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We can flip this around: hold the metric fixed and present evidence in favour of a grammar.

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Example: hold self-embedding fixed as the complexity metric.

(4) That [the food that [John ordered] tasted good] pleased him.

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Proposed answer	(4) structure	(5) structure	Prediction
Yes	. . . [S . . . [S . . .]]	. . . [S . . . [S . . .]]	(4) & (5) same
No	. . . [S . . . [RC . . .]]	. . . [S . . . [S . . .]]	(5) harder

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Conclusion: The fact that (5) is harder supports the "No" answer.

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Derivations and representations

Question

But these metrics are all properties of a final, fully-constructed tree.
How can anything like this be sensitive to differences in the derivational operations that build these trees? (e.g. TAG vs. MG, whether move is re-merge)

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- minimal attachment, late closure, etc.?
- "nature, number and complexity of" transformations (Miller and Chomsky 1963)

"nature, number and complexity of the grammatical transformations involved"

The psychological plausibility of a transformational model of the language user would be strengthened, of course, if it could be shown that our performance on tasks requiring an appreciation of the structure of transformed sentences is ***some function of the nature, number and complexity of the grammatical transformations involved****.*

(Miller and Chomsky 1963: p.481)

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Answer

The relevant objects on which the interpretation functions are defined encode a complete derivational history.

e.g. The function which, given a complete "recipe" for carrying out a derivation, returns the number of movement steps called for by the recipe.
(Maybe only useful when we're holding a grammar fixed)

Full derivation recipes?

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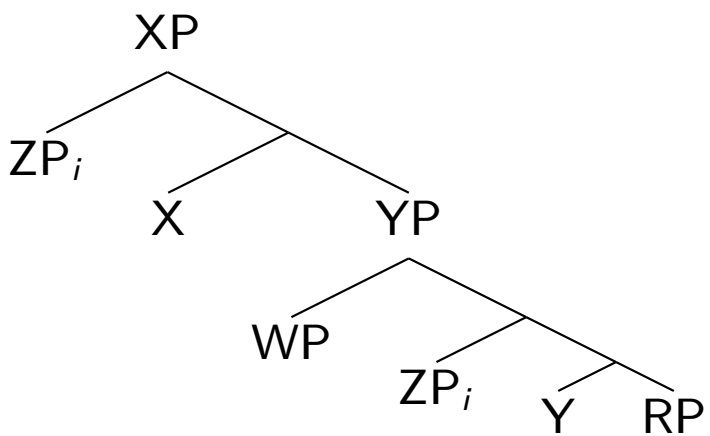

- merge Y with RP
- merge the result with ZP
- merge the result with WP
- merge X with the result
- move ZP

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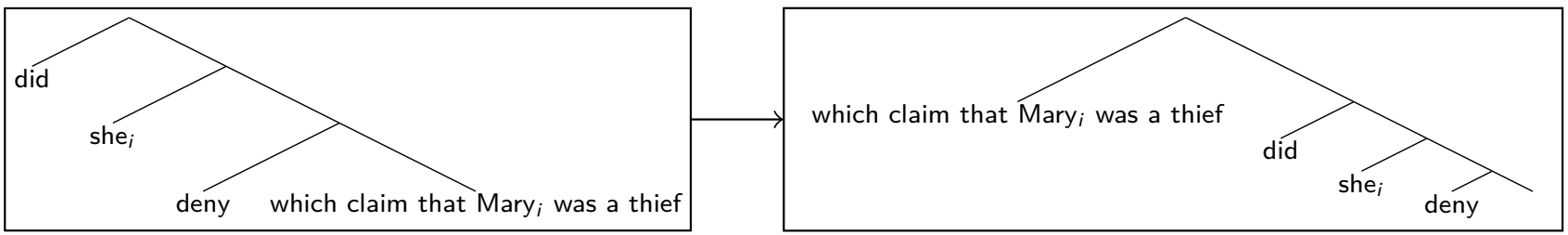

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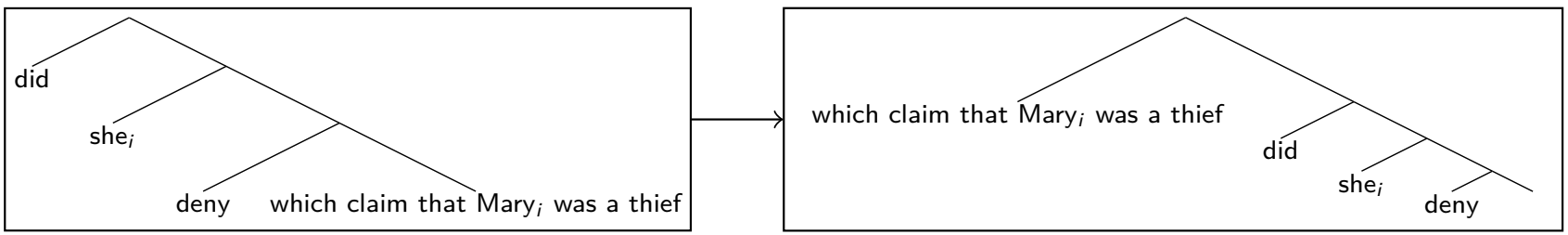

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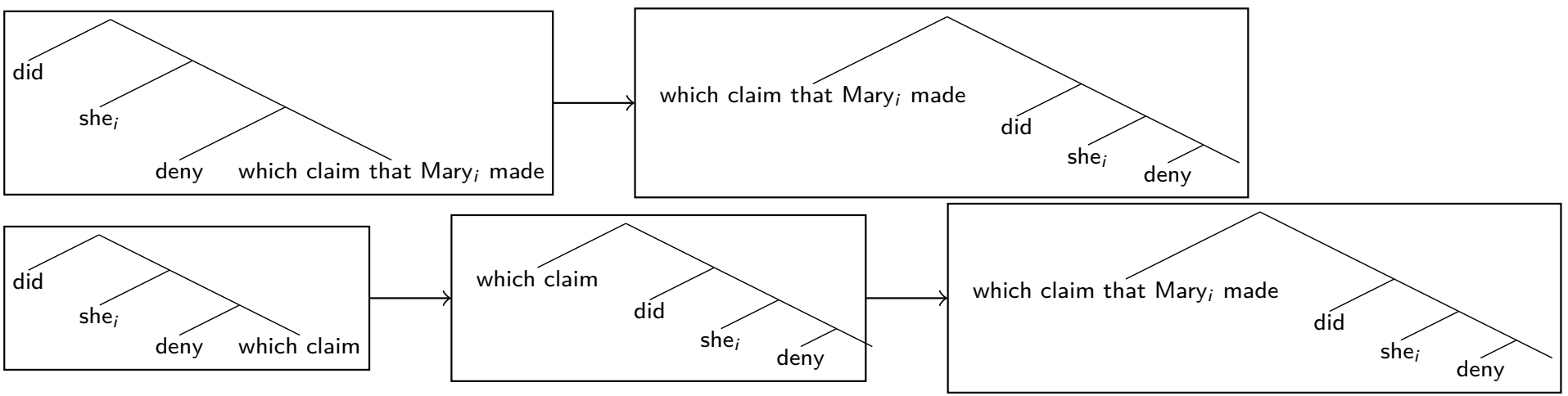

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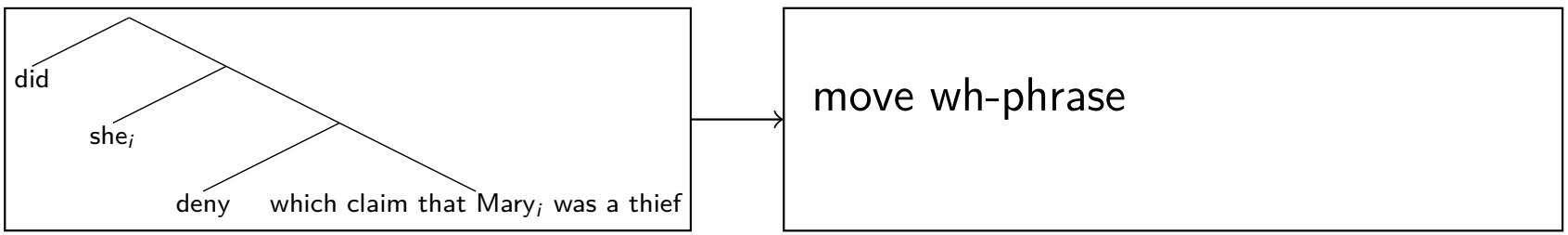

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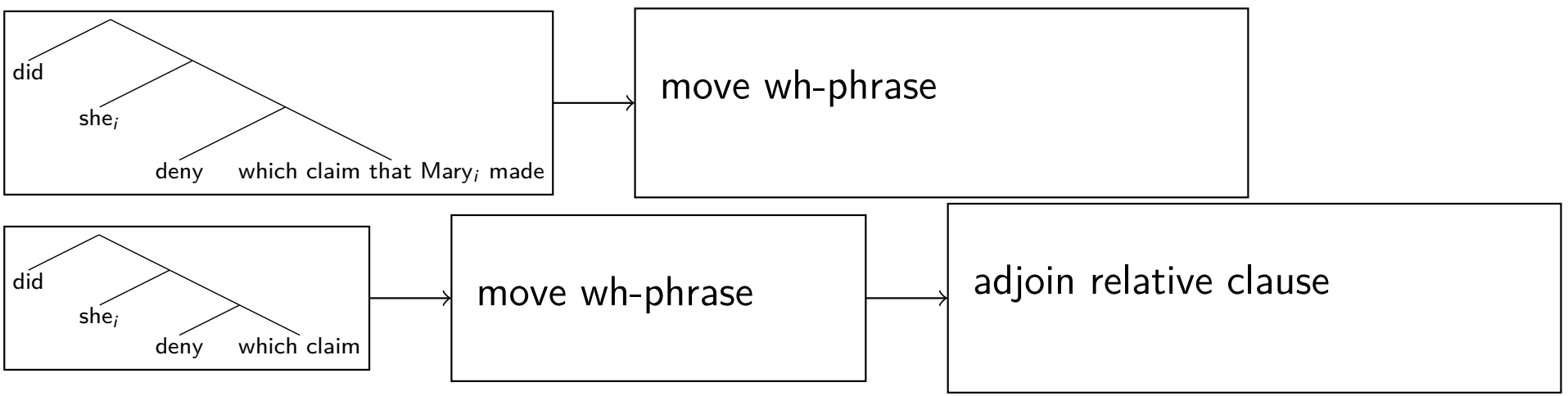

Full derivation recipes?

Also:

- subjacency effects without traces
- compare categorial grammar

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And this is not a new idea!

> *[The perceptual model] will utilize the full resources of the transformational grammar to provide a structural description, consisting of a set of P-markers and a transformational history*
>
> *Miller and Chomsky (1963: p.480)*

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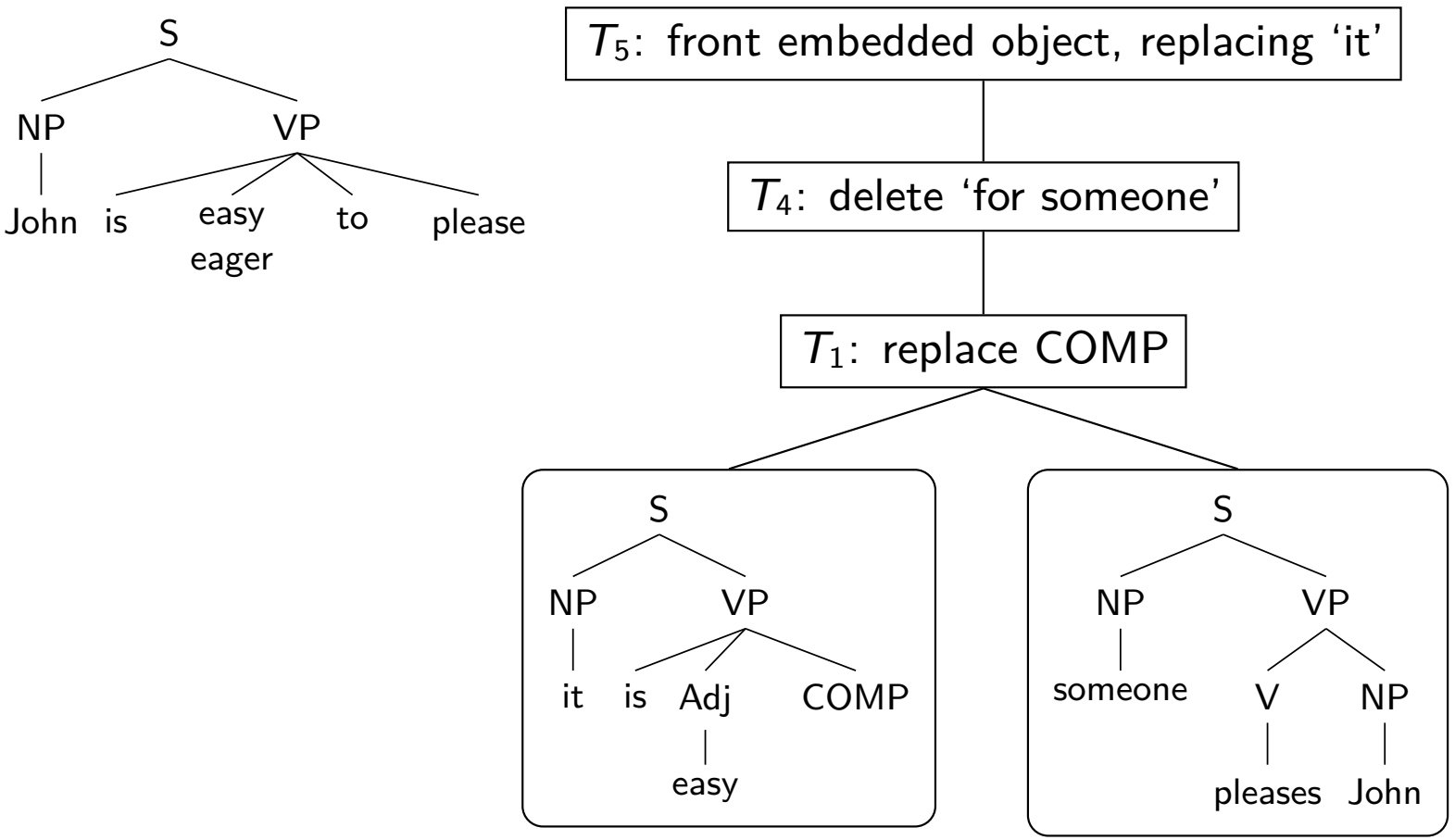

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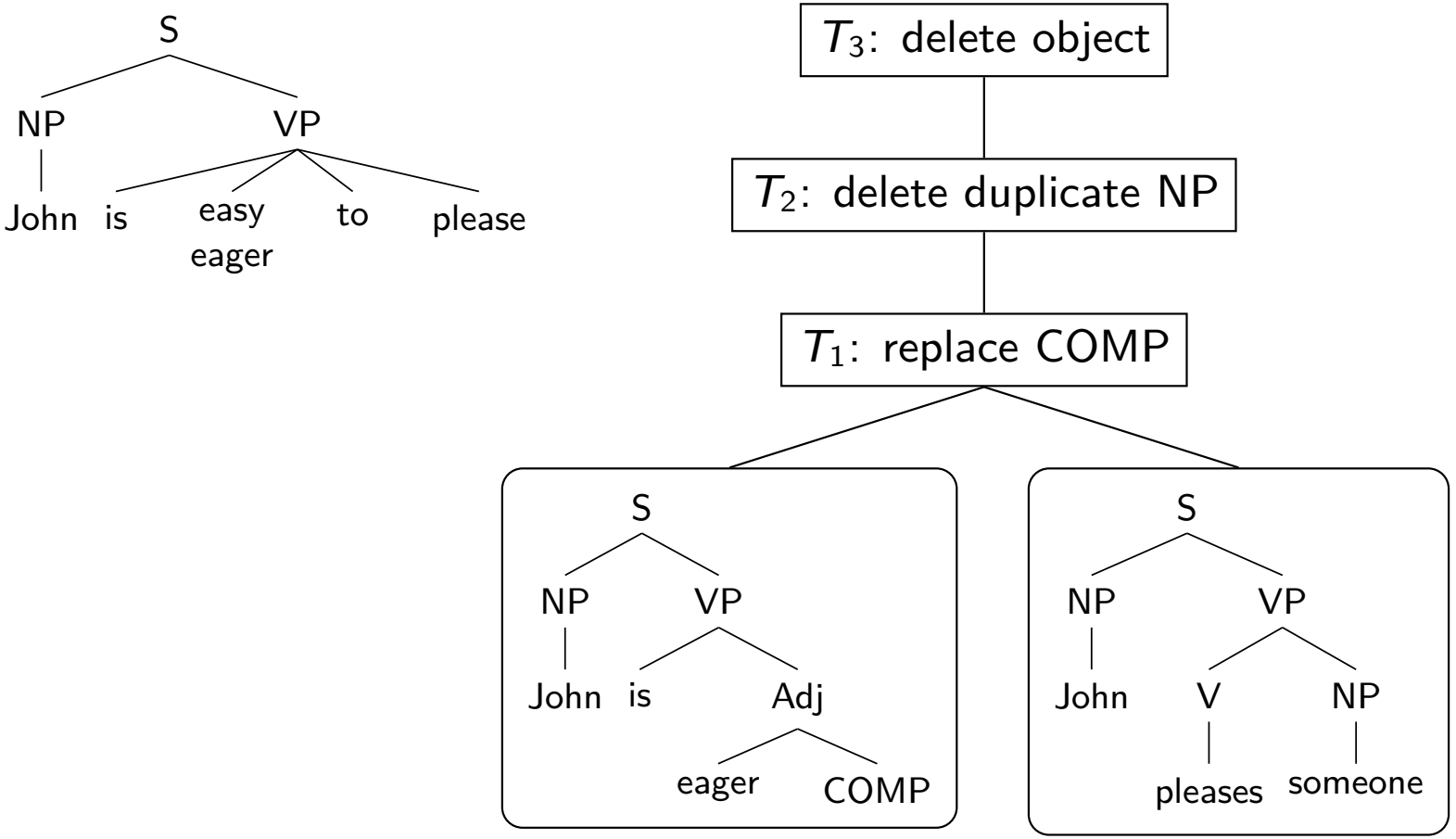
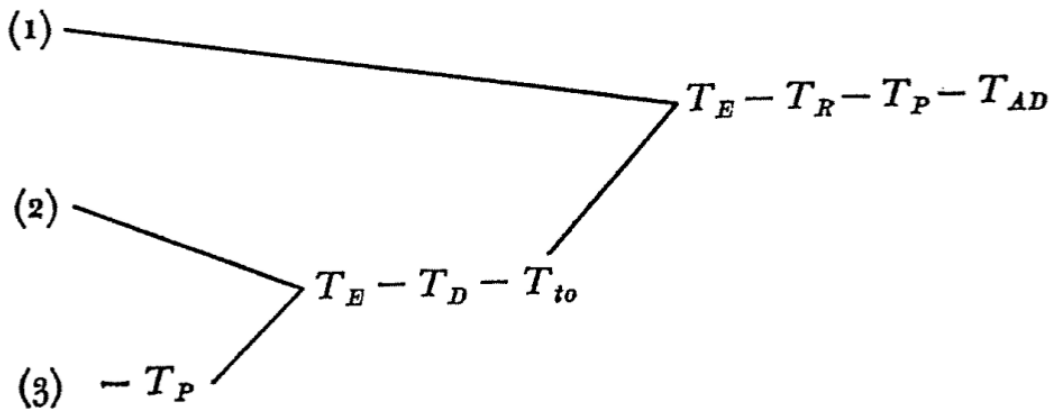


Full derivation recipes?

(4) the man who persuaded John to be examined by a specialist was fired

The "transformational history" of (4) by which it is derived from its basis might be represented, informally, by the diagram (5).

(5)



(Chomsky 1965)

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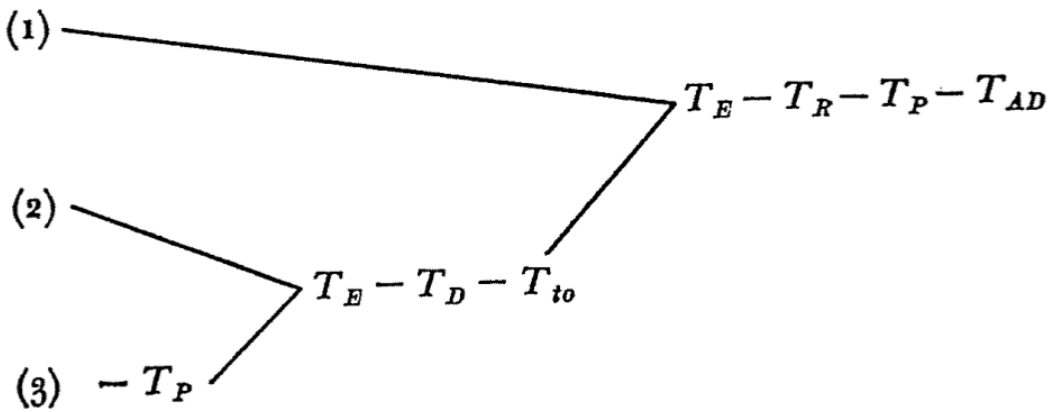

Differences these days:

- We'll have things like merge and move at the internal nodes instead of T_P, T_E, etc.
- We'll have lexical items at the leaves rather than base-derived trees.

(Chomsky 1965)

Outline

Surprisal and entropy reduction

Why these complexity metrics?

- Partly just for concreteness, to give us a goal.
- They are formalism neutral to a degree that others aren't.
- They are mechanism neutral (Marr level one).
- The pieces of the puzzle that we need to get there (e.g. probabilities) seem likely to be usable in other ways.

Surprisal and entropy reduction

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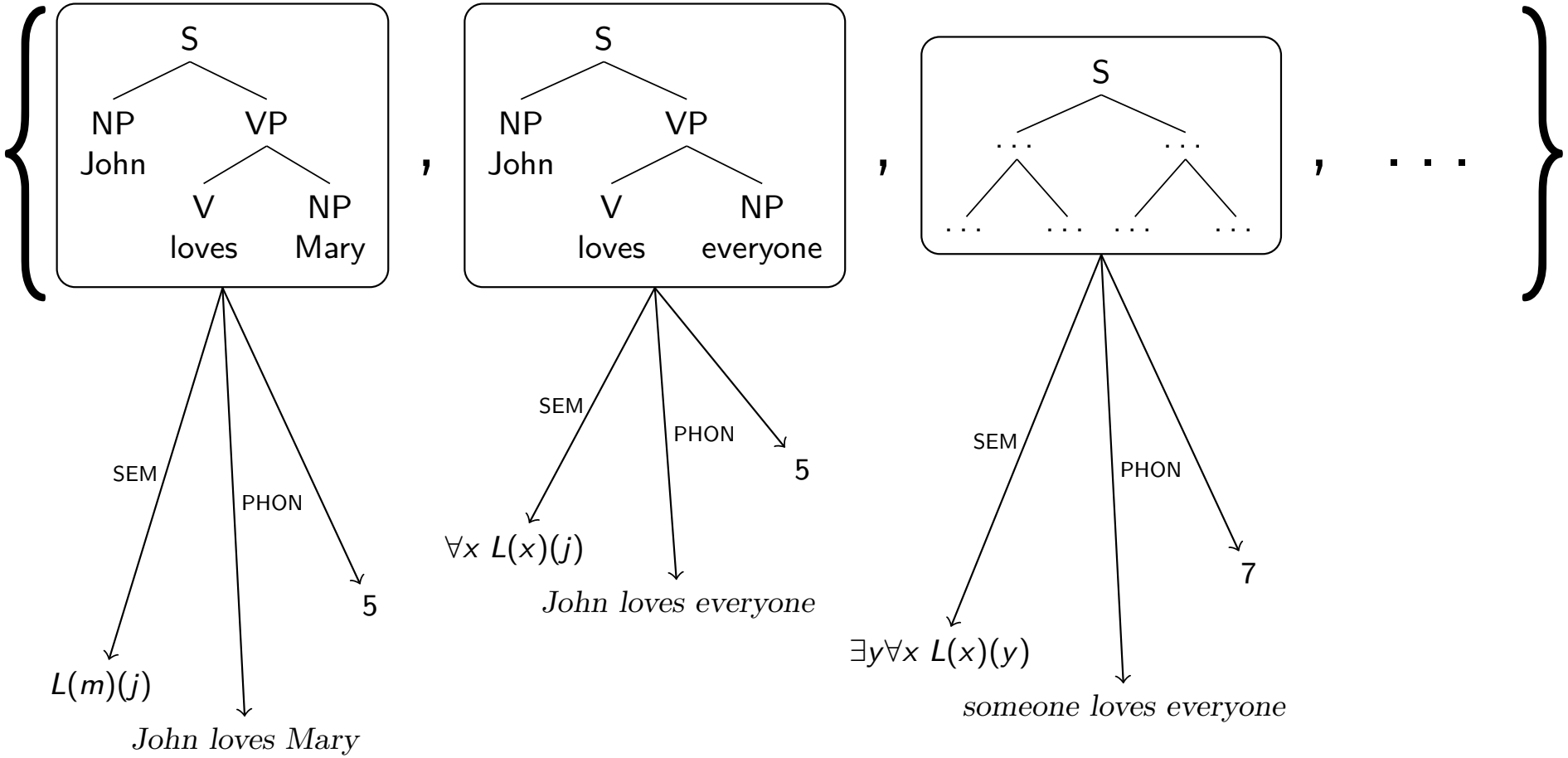
John Hale, Cornell Univ.

Interpretation functions



Caveats:

- Maybe we're interested in the finite specification of the set
- Maybe there's no clear line between observable and not
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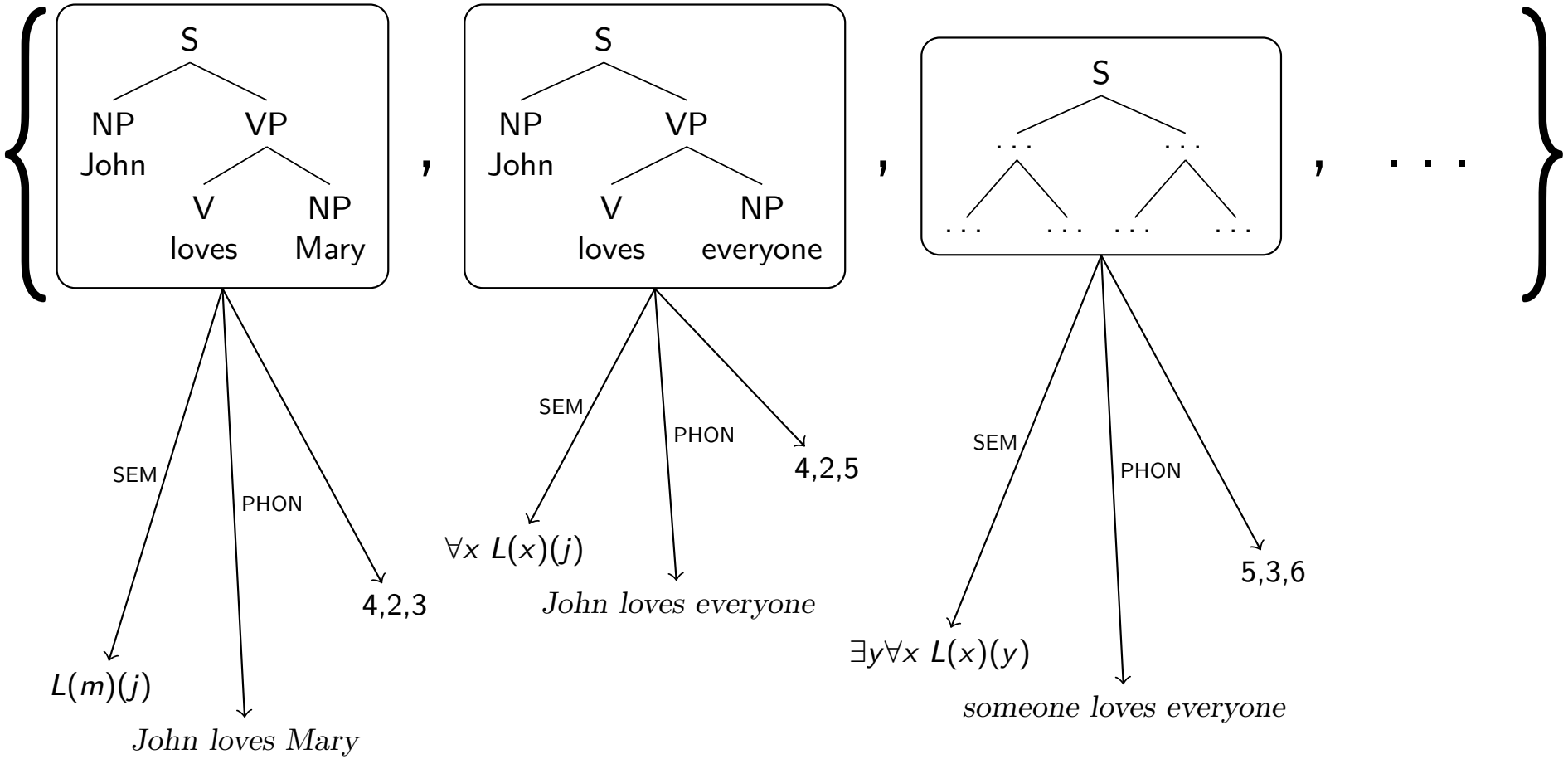

Caveats:

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- Maybe there's no clear line between observable and not
- Maybe some evidence is based on relativities among interpretations

Surprisal

Given a sentence $w_1 w_2 \ldots w_n$:

$$\text{surprisal at } w_i = -\log P(W_i = w_i \mid W_1 = w_1, W_2 = w_2, \ldots, W_{i-1} = w_{i-1})$$

Surprisal

0.4	John ran
0.15	John saw it
0.05	John saw them
0.25	Mary ran
0.1	Mary saw it
0.05	Mary saw them

What predictions can we make about the difficulty of comprehending 'John saw it'?

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$$\begin{aligned}\text{surprisal at 'John'} &= -\log P(W_1 = \text{John}) \\ &= -\log(0.4 + 0.15 + 0.05) \\ &= -\log 0.6 \\ &= 0.74\end{aligned}$$

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$$\begin{aligned}\text{surprisal at 'saw'} &= -\log P(W_2 = \text{saw} \mid W_1 = \text{John}) \\ &= -\log \frac{0.15 + 0.05}{0.4 + 0.15 + 0.05} \\ &= -\log 0.33 \\ &= 1.58\end{aligned}$$

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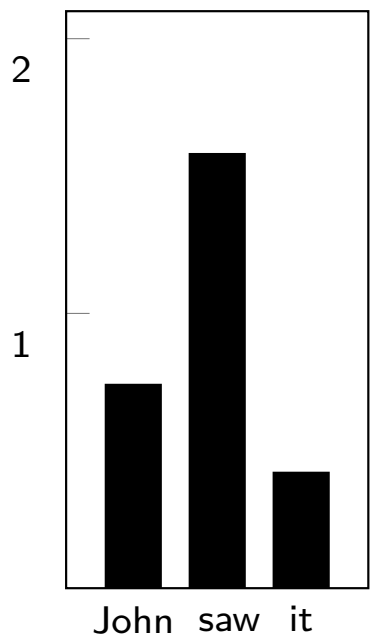
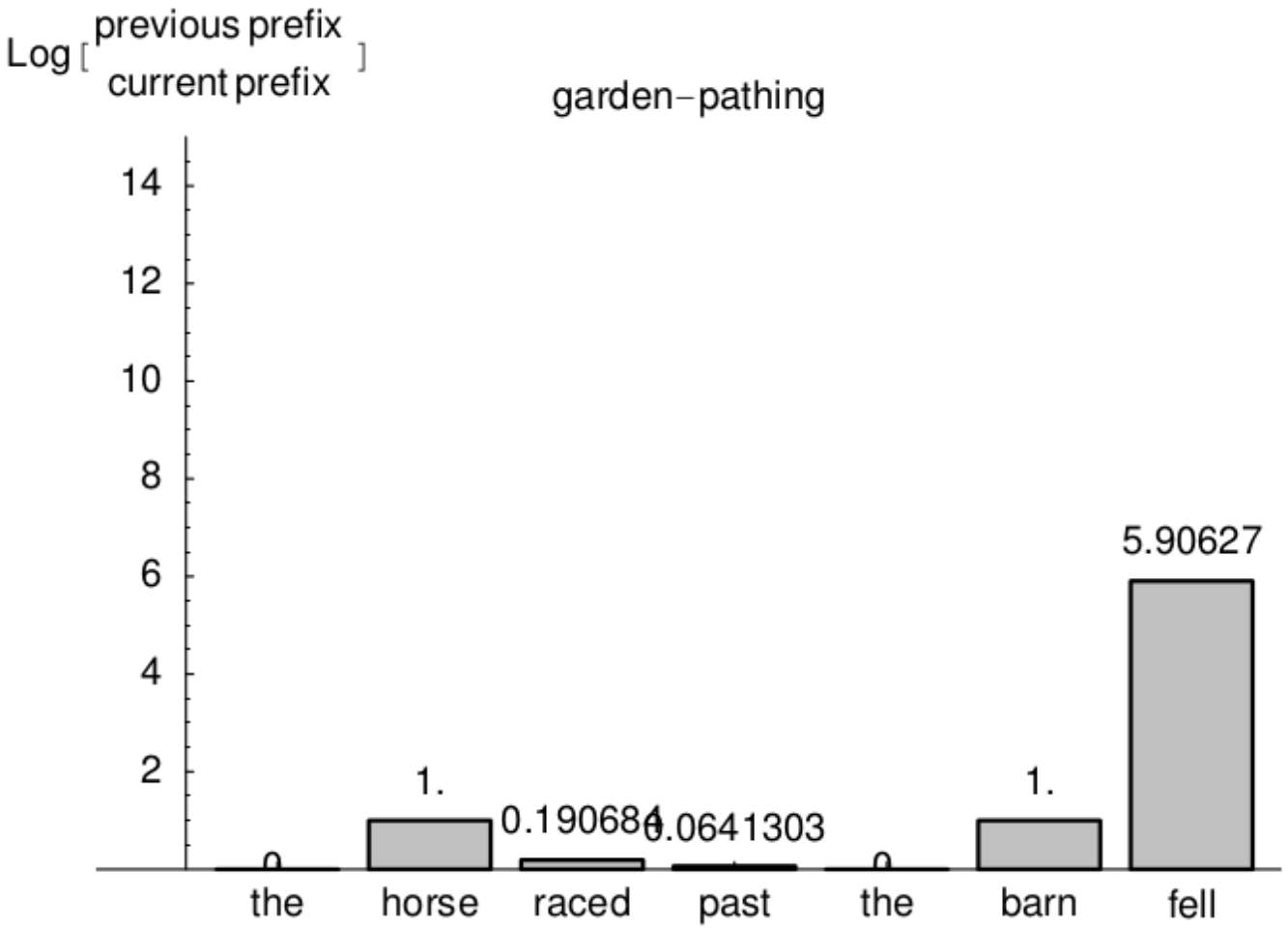
$$\begin{aligned}\text{surprisal at 'it'} &= -\log P(W_3 = \text{it} \mid W_1 = \text{John}, W_2 = \text{saw}) \\ &= -\log \frac{0.15}{0.15 + 0.05} \\ &= -\log 0.75 \\ &= 0.42\end{aligned}$$



Accurate predictions made by surprisal

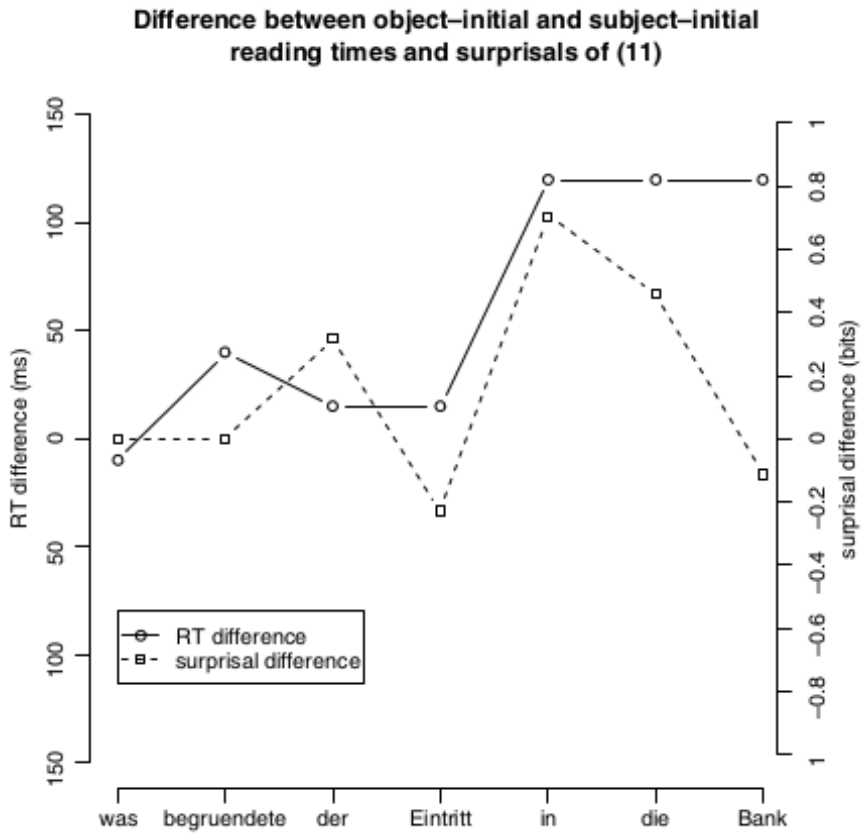


(Hale 2001)

Accurate predictions made by surprisal

(8) The reporter [who ____ attacked the senator] left the room. (easier)

(9) The reporter [who the senator attacked ____] left the room. (harder)



(Levy 2008)

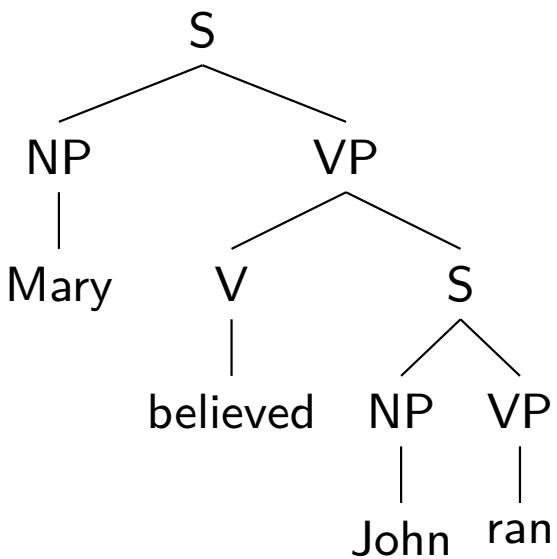
An important distinction

Using surprisal as a complexity metric says nothing about the form of the knowledge that the language comprehender is using!

- We're asking "what's the probability of w_i, given that we've seen $w_1 \ldots w_{i-1}$ in the past".
- This does not mean that the comprehender's knowledge takes the form of answers to this kind of question.
- The linear nature of the metric reflects the task, not the knowledge being probed.

Probabilistic CFGs

1.0	S → NP VP
0.3	NP → John
0.7	NP → Mary
0.2	VP → ran
0.5	VP → V NP
0.3	VP → V S
0.4	V → believed
0.6	V → knew



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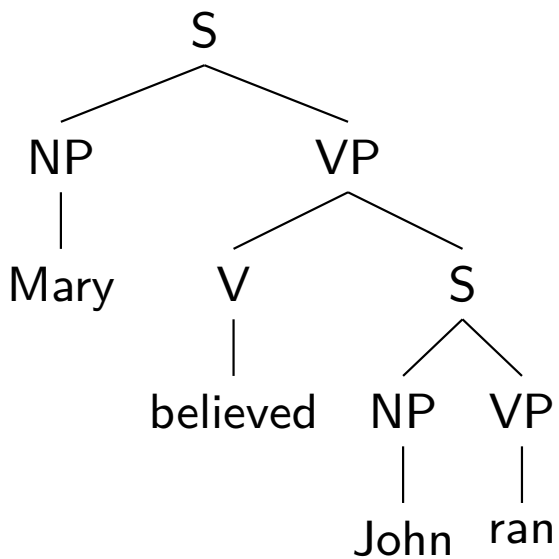

$$P(\text{Mary believed John ran}) = 1.0 \times 0.7 \times 0.3 \times 0.4 \times 1.0 \times 0.3 \times 0.2$$
$$= 0.00504$$

Surprisal with probabilistic CFGs

Goal: Calculate step-by-step surprisal values for 'Mary believed John ran'

surprisal at 'John' $= -\log P(W_3 = \text{John} \mid W_1 = \text{Mary}, W_2 = \text{believed})$

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0.098	**Mary believed** Mary
0.042	**Mary believed** John
0.012348	**Mary believed** Mary knew Mary
0.01176	**Mary believed** Mary ran
0.008232	**Mary believed** Mary believed Mary
0.005292	**Mary believed** Mary knew John
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0.00504	**Mary believed** John ran
...	...

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...	...

There are an infinite number of derivations consistent with input at each point!

$$\begin{aligned}\text{surprisal at 'John'} &= -\log P(W_3 = \text{John} \mid W_1 = \text{Mary}, W_2 = \text{believed}) \\ &= -\log \frac{0.042 + 0.005292 + 0.00504 + \ldots}{0.098 + 0.042 + 0.12348 + 0.01176 + 0.008232 + \ldots}\end{aligned}$$

Intersection grammars

1.0	S → NP VP
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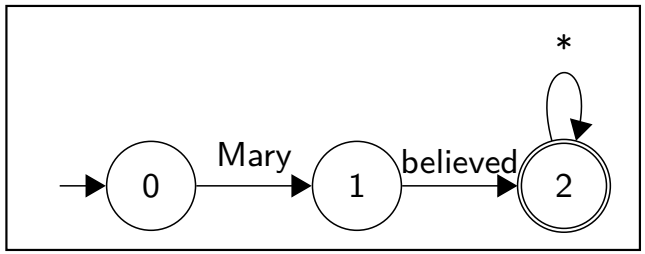
$\cap$



$=$ G_2

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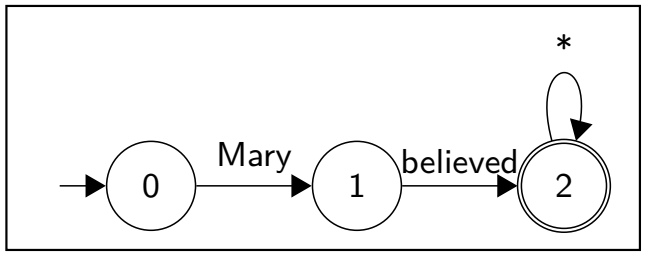

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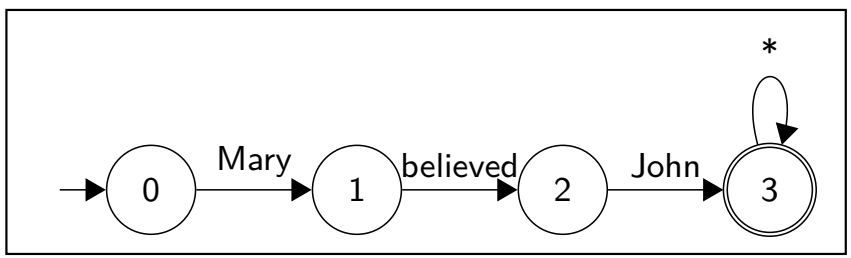

$=$ G_3

Intersection grammars

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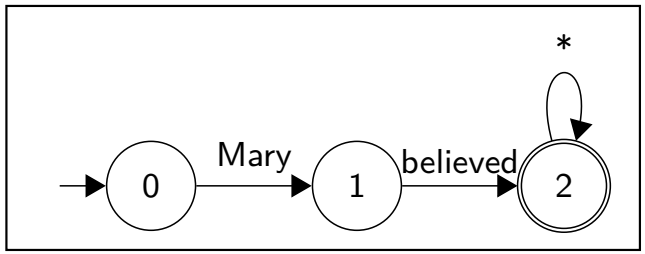
$\cap$



$= G_2$

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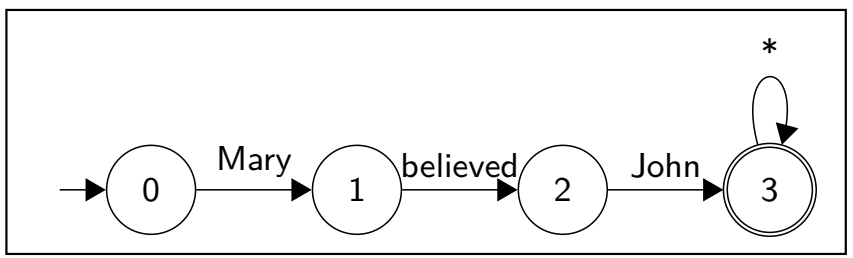

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\text{surprisal at 'John'} &= -\log P(W_3 = \text{John} \mid W_1 = \text{Mary}, W_2 = \text{believed}) \\
&= -\log \frac{\text{total weight in } G_3}{\text{total weight in } G_2} \\
&= -\log \frac{0.0672}{0.224} \\
&= 1.74
\end{aligned}$$

Grammar intersection example (simple)

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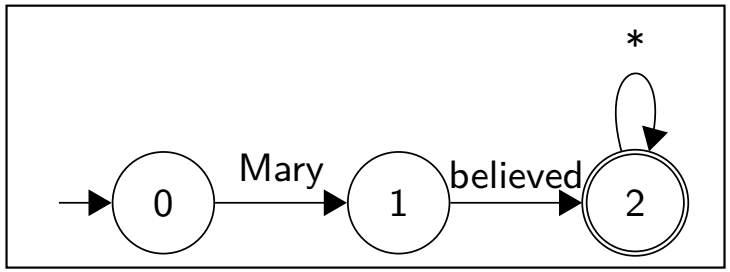

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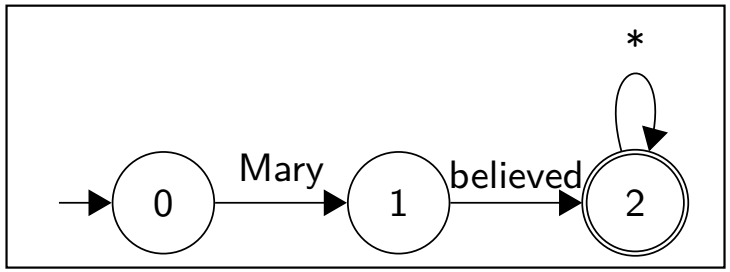

1.0	$S_{0,2}$	→	$NP_{0,1}$ $VP_{1,2}$
0.7	$NP_{0,1}$	→	Mary
0.5	$VP_{1,2}$	→	$V_{1,2}$ $NP_{2,2}$
0.3	$VP_{1,2}$	→	$V_{1,2}$ $S_{2,2}$
0.4	$V_{1,2}$	→	believed

1.0	$S_{2,2}$	→	$NP_{2,2}$ $VP_{2,2}$
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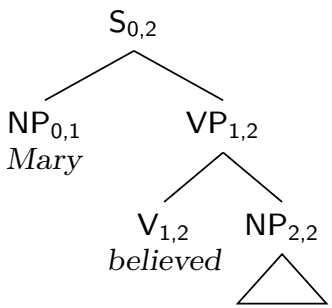
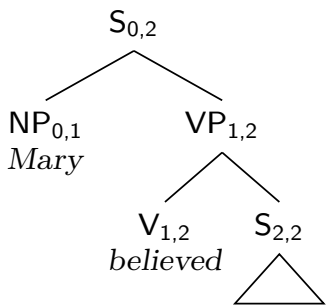
0.7	$NP_{2,2}$	→	Mary
0.2	$VP_{2,2}$	→	ran
0.5	$VP_{2,2}$	→	$V_{2,2}$ $NP_{2,2}$
0.3	$VP_{2,2}$	→	$V_{2,2}$ $S_{2,2}$
0.4	$V_{2,2}$	→	believed
0.6	$V_{2,2}$	→	knew



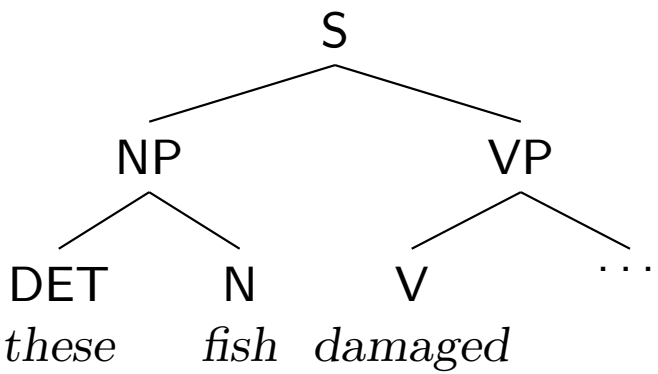


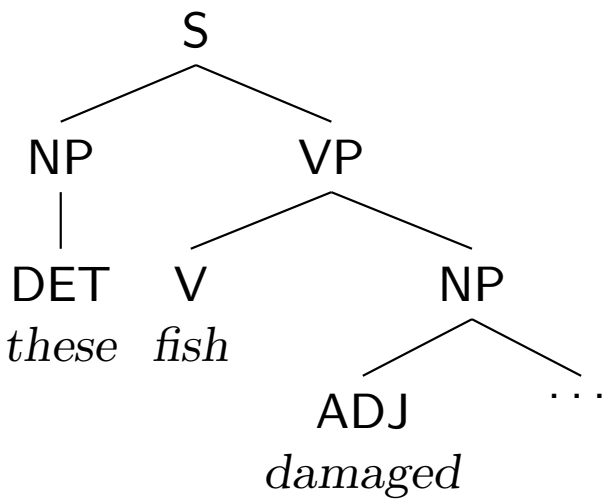
NB: Total weight in this grammar is not one! (What is it? Start symbol is $S_{0,2}$.)
Each derivation has the weight "it" had in the original grammar.

Grammar intersection example (more complicated)

S	$\rightarrow$	NP VP	V	$\rightarrow$	*fish*
VP	$\rightarrow$	V NP	V	$\rightarrow$	*damaged*
NP	$\rightarrow$	DET	DET	$\rightarrow$	*these*
NP	$\rightarrow$	DET N	N	$\rightarrow$	*fish*
NP	$\rightarrow$	ADJ N	ADJ	$\rightarrow$	*damaged*

These fish damaged . . .





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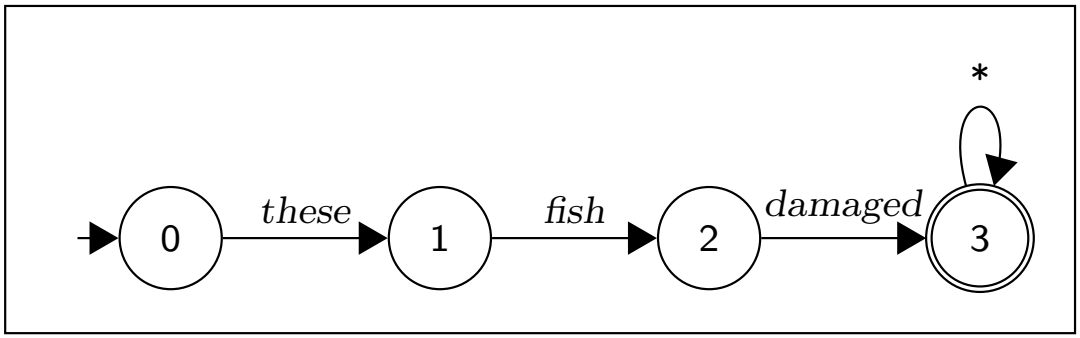
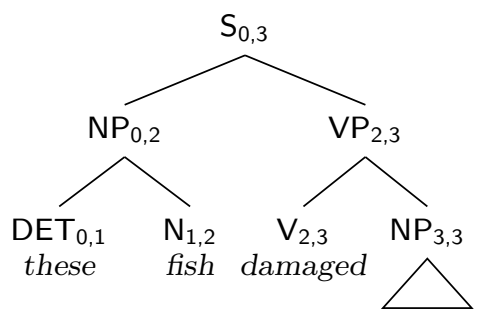
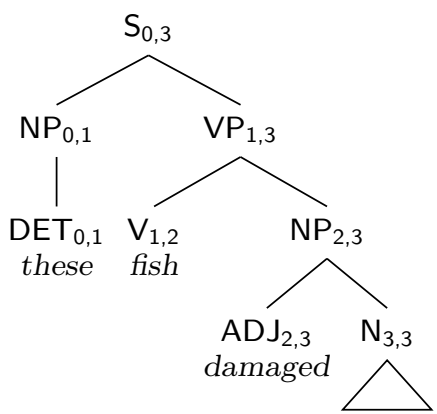


$S_{0,3}$	→	$NP_{0,2}$ $VP_{2,3}$	$S_{0,3}$	→	$NP_{0,1}$ $VP_{1,3}$	$NP_{3,3}$	→	$ADJ_{3,3}$ $N_{3,3}$
$NP_{0,2}$	→	$DET_{0,1}$ $N_{1,2}$	$NP_{0,1}$	→	$DET_{0,1}$	$NP_{3,3}$	→	$DET_{3,3}$ $N_{3,3}$
$VP_{2,3}$	→	$V_{2,3}$ $NP_{3,3}$	$VP_{1,3}$	→	$V_{1,2}$ $NP_{2,3}$	$NP_{3,3}$	→	$DET_{3,3}$
$DET_{0,1}$	→	*these*	$NP_{2,3}$	→	$ADJ_{2,3}$ $N_{3,3}$	$N_{3,3}$	→	*fish*
$N_{1,2}$	→	*fish*	$V_{1,2}$	→	*fish*	$DET_{3,3}$	→	*these*
$V_{2,3}$	→	*damaged*	$ADJ_{2,3}$	→	*damaged*	$ADJ_{3,3}$	→	*damaged*





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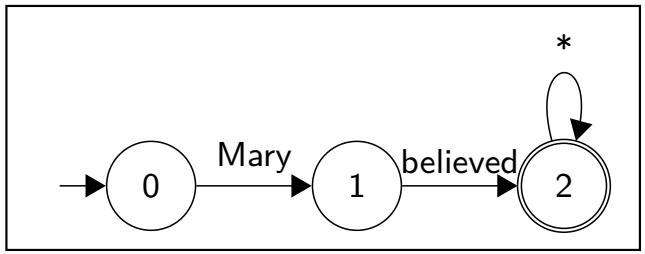

$= G_2$

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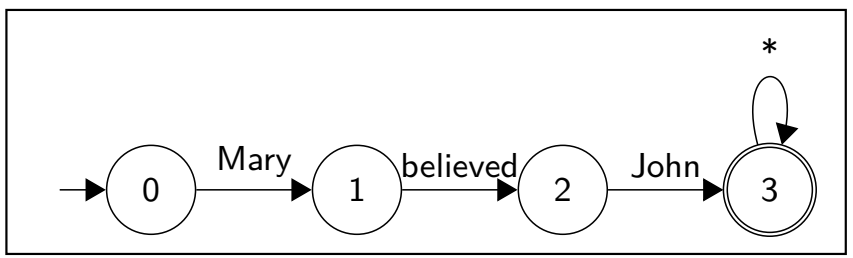

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Computing sum of weights in a grammar ("partition function")

$$Z(A) = \sum_{A \to \alpha} \Big(p(A \to \alpha) \cdot Z(\alpha) \Big)$$

$$Z(\epsilon) = 1$$

$$Z(a\beta) = Z(\beta)$$

$$Z(B\beta) = Z(B) \cdot Z(\beta) \qquad \text{where } \beta \neq \epsilon$$

(Nederhof and Satta 2008)

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$$Z(\text{V}) = 0.4 + 0.6 = 1.0$$

$$Z(\text{NP}) = 0.3 + 0.7 = 1.0$$

$$Z(\text{VP}) = 0.2 + (0.5 \cdot Z(\text{V}) \cdot Z(\text{NP}))$$

$$= 0.2 + (0.5 \cdot 1.0 \cdot 1.0) = 0.7$$

$$Z(\text{S}) = 1.0 \cdot Z(\text{NP}) \cdot Z(\text{VP})$$

$$= 0.7$$

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$$Z(\text{NP}) = 0.3 + 0.7 = 1.0$$

$$Z(\text{VP}) = 0.2 + (0.5 \cdot Z(\text{V}) \cdot Z(\text{NP}))$$

$$= 0.2 + (0.5 \cdot 1.0 \cdot 1.0) = 0.7$$

$$Z(\text{S}) = 1.0 \cdot Z(\text{NP}) \cdot Z(\text{VP})$$

$$= 0.7$$

1.0	S → NP VP
0.3	NP → John
0.7	NP → Mary
0.2	VP → ran
0.5	VP → V NP
0.3	VP → V S
0.4	V → believed
0.6	V → knew

$$Z(\text{V}) = 0.4 + 0.6 = 1.0$$

$$Z(\text{NP}) = 0.3 + 0.7 = 1.0$$

$$Z(\text{VP}) = 0.2 + (0.5 \cdot Z(\text{V}) \cdot Z(\text{NP})) + (0.3 \cdot Z(\text{V}) \cdot Z(\text{S}))$$

$$Z(\text{S}) = 1.0 \cdot Z(\text{NP}) \cdot Z(\text{VP})$$

Things to know

Technical facts about CFGs:

- Can intersect with a "prefix FSA"
- Can compute the total weight (and the entropy)

(Hale 2006)

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More generally:

- Intersecting a grammar with a prefix produces a new grammar which is a representation of the comprehender's sentence-medial state
- So we can construct a sequence of grammars which represents the comprehender's sequence of knowledge-states
- Ask "what changes" (or "how much changes", etc.) at each step

The general approach is compatible with many very different grammar formalisms (any grammar formalism?) — provided the technical tricks can be pulled off.

(Hale 2006)

Looking ahead

Wouldn't it be nice if we could do all that for minimalist syntax?

The average syntax paper shows illustrative derivations, not a fragment.

What would we need?

- An explicit characterization of the set of possible derivations
- A way to "intersect" that with a prefix
- A way to define probability distributions over the possibilities

This will require certain idealizations. (But what's new?)

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