7. Minimalist Grammars (MGs)

1 Derivation trees

Thinking back to our "even number of as" FSTA, for example, we indicated the role of *states* as in (1). A more verbose way of expressing the same thing would be (2).



A representation like (2) is redundant here, because in the case of an FSTA we can always identify the **derivational antecedents** of a tree by looking at its **subparts**.

In MGs, an expression's derivational antecedents *do not* always coincide with its subparts, so representations like (2) are not redundant in this way.

2 MG basics

MGs were originally defined in Stabler 1997; a good overview is in Stabler 2011. Many of the examples here are from the introductory chapter of Graf 2013.

MGs are a completely lexicalized formalism: a grammar for a particular language just is a collection of lexical items. A small example grammar (based on Graf 2013, p.12) is given in (3).

(3)	the ::= N D	pigs :: N	$\varepsilon ::= \!\! V = \!\! D v$
	the ::= N D - nom	$\verb+sleep::V$	$\varepsilon ::= v + nom T$
	which $::= N D - wh$	$\texttt{kiss} ::= D \ V$	$\mathtt{that} ::= T \ C$
	which ::= N D - nom - wh	owe ::= D = D V	$\varepsilon ::= T C$
	's::=N =D D	tell ::= C = D V	$\varepsilon ::= T + wh C$

The pieces of information on each lexical item that specify what can combine with what are called **features**.

- Merge checks a *selector feature*, written =F, and a *category feature*, written F.
- Move checks a *licensor feature*, written +F, and a *licensee feature*, written -F.
- The head of each newly-formed constituent is the element that had a selector feature (in the case of merge) or licensor feature (in the case of move) checked.
- The features on a lexical item **must be checked in order** (starting with the leftmost). So bringing a lexical item into a derivation commits you to a certain ordered bundle of derivational operations: a merge step for each selector/category feature, and a move step for each licensor/licensee feature.

If the element having a selector (=X) feature checked by merge is a lexical item (i.e. a trivial, one-node tree), then it becomes the left daughter of the resulting tree.



If the element having a selector (=X) feature checked by merge is a complex tree, then it becomes the right daughter of the resulting tree.



The element having a licensee (-X) feature checked by merge becomes the left daughter of the resulting tree.

(6)



Here's one very simple derivation (from Graf 2013, pp.13–18).





Here's a more interesting example involving remnant movement (Graf, 2013, pp.19–20).

3 The Shortest Move Constraint (SMC)

- The SMC is often presented (e.g. Stabler, 1997, 2011) as a part of the definition of the move operation: move can apply to an expression iff
 - $\circ~$ the first feature on the expression's head is a licensor feature, and
 - there is *exactly one* subconstituent whose first feature is a matching licensee feature.
- A consequence of this, however, is that if we ever find ourselves with two "competing" licensee features on subconstituents of a single expression, there will be no way to check either of them, and so such an expression is doomed. So the SMC can equivalently be stated as a ban on expressions where licensee features "compete" in this way (Graf, 2013, p.25).
- For example, if +/-nom and +/-acc in (8) were replaced by simply +/-case, we would end up with two competing -case licensee features after Hans is merged, and that derivation would be doomed.

4 Derivations are finite-state

The SMC guarantees that an MG's derivations are finite-state.

4.1 What information matters?

First, notice that it suffices to keep track of:

- the feature-sequence on the current head, and
- the feature-sequences on any other subconstituents.

The part that's slightly unintuitive, at first, is that it's not important to keep track of *where* the subconstituents with unchecked features are. The reason this is not important is that they *must* move out of their current positions.

Here's a tree which shows just the states that the derivation in (8) transitions through.

(9) (C)

$$(+ \operatorname{top} C, -\operatorname{top})$$

hat :: =T +top C (T, -top)
 $(+ \operatorname{nom} T, -\operatorname{nom}, -\operatorname{top})$
 $(+ \operatorname{nom} T, -\operatorname{nom}, -\operatorname{top})$
 $(+ \operatorname{acc} v, -\operatorname{acc}, -\operatorname{nom}, -\operatorname{top})$
 $(+ \operatorname{acc} v, -\operatorname{acc}, -\operatorname{nom}, -\operatorname{top})$
 $(= D + \operatorname{acc} v, -\operatorname{acc}, -\operatorname{top})$
Hans :: D -nom
 ε :: =V =D + \operatorname{acc} v (V -top, -acc)
gelesen :: =D V -top (D - acc)
 das :: =N D - acc Buch :: N

4.2 How many distinctions are there?

Then, the SMC ensures that only finitely many of these tuples-of-feature-sequences (i.e. states) are needed:

- Each component of the tuples is a suffix of a lexical item's feature-sequence, so there are only finitelymany possibilities in each slot.
- There is a finite bound on the number of slots namely, the number of licensee feature types plus one.
 - $\circ~$ If any component other than the initial component contains anything other than licensee features, the derivation is doomed.
 - $\circ\,$ If any two of these non-initial components both start with –F, for some particular feature type F, then the derivation is doomed.
 - $\circ\,$ So the biggest possible tuple contains an initial component, plus one additional component for each distinct type of licensee feature.

5 Where does the non-context-freeness come from, exactly?

Unsurprisingly, MGs without move generate only the context-free string languages: in such an MG, the finite-state derivational process doesn't "disrupt" existing tree structure at all, so it's essentially an FSTA.

More interestingly: MGs with only "one at a time" phrasal movement (e.g. if there is only one movement feature type) also only generate context-free string languages, because the effects of this limited kind of structural disruption can be mimicked by an FSTA/CFG.

(10)



For an MG to generate a non-context-free string language, it needs to allow the distortions created by movement to *accumulate*. Remnant movement or head movement can do this.

Here's a grammar that generates the flip/flop/tick/tock crossing-dependencies language, using remnant movement.

(11) $\varepsilon :: S - r - l$ $\varepsilon :: = S + r + l S$ flop :: = S + r F - r tock :: = S + r T - r flip :: = F + l S - l tick :: = T + l S - l





The key idea is that this grammar allows for "derivational loops" like this:

In effect, remnant movement allows us to work at the roots of two independent subtrees.



This is the fundamental difference that allows MGs to go beyond FSTAs: FSTAs categorize *individual trees* that grow bottom-up, whereas **MGs categorize** *tuples of trees* that grow bottom-up.

This also underlies the equivalence between MGs and *Multiple Context-Free Grammars* (MCFGs), which operate over *tuples of strings*; see e.g. Hunter and Dyer 2013, §2 for a brief explanation of this.

References

Graf, T. (2013). Local and transderivational constraints in syntax and semantics. PhD thesis, UCLA.

- Hunter, T. and Dyer, C. (2013). Distributions on Minimalist Grammar derivations. In Proceedings of the 13th Meeting on the Mathematics of Language.
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